Correlation between *p*-type conductivity and electronic structure of Cr-deficient $CuCr_{1-x}O_2$ (x = 0-0.1)

Shashi B. Singh, L. T. Yang, Y. F. Wang, Y. C. Shao, C. W. Chiang, J. W. Chiou, K. T. Lin, S. C. Chen, B. Y. Wang, C. H. Chuang, D. C. Ling, H. W. F. Pong, M. H. Tsai, H. M. Tsai, C. W. Pao, H. W. Shiu, C. H. Chen, H.-J. Lin, J. F. Lee, H. Yamane, and N. Kosugi Department of Physics, Tamkang University, Tamsui 251, Taiwan

Department of Applied Physics, National University of Kaohsiung, Kaohsiung 811, Taiwan

Department of Physics, National Sun Yat-Sen University, Kaohsiung 804, Taiwan

Mational Synchrotron Radiation Research Center, Hsinchu 300, Taiwan

Institute for Molecular Science, Okazaki 444-8585, Japan

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The correlation between the p-type hole conduction and the electronic structures of Cr-deficient $CuCr_{1-x}O_2$ (x=0-0.1) compounds was investigated using O K-, Cu, and Cr $L_{3,2}$ -edge x-ray absorption near-edge structure (XANES), scanning photoelectron microscopy, and x-ray emission spectroscopy measurements. XANES spectra reveal a gradual increase in the Cu valence from Cu^{1+} to Cu^{2+} with increasing Cr deficiency x, whereas, the valence of Cr remains constant as Cr^{3+} . These results indicate that the p-type conductivity in the $CuCr_{1-x}O_2$ samples is enhanced by a Cu^{1+} -O- Cu^{2+} rather than a Cr^{3+} - Cr^{4+} or direct Cu^{1+} - Cu^{2+} hole mechanism. Remarkable Cr-deficiency-induced changes in the densities of Cu 3d, Cu 3d-O 2p, and O 2p states at or near the valence-band maximum or the Fermi level were also observed. In addition, a crossover of conduction mechanism from thermally activated (TA) hopping to a combination of TA and Mott's three-dimensional variable range hopping occurs around 250 K.

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Delafossite oxides, $CuMO_2$ (M = trivalent metal cations), have recently attracted much interest because of their intriguing magnetoelectric properties, making them promising candidates for new optoelectronic and spin-based device applications. 1,2 These compounds contain a two-dimensional triangular lattice composed of $M^{3+}O_2$ in which the layers of edge-sharing MO₆ octahedra lie parallel to the ab plane; the Cu¹⁺ ions are linearly connected to two O ions that are alternately stacked along the c axis³ (see the Supplemental Material of Fig. S1 in Ref. 4). Among them, CuCrO₂ has attracted considerable attention due to its favorable transport properties. It has been suggested that the observed higher conductivity of CuCrO2 than that of other delafossites may arise from the mixing of Cr 3d and O 2p states in the Cr^{3+} -O-Cu¹⁺ linkages.⁵ Theoretical calculations using the augmented spherical wave method showed that the density of states (DOS) of CuCrO₂ at or near the valence-band maximum (VBM) or the Fermi level $(E_{\rm f})$ is composed mainly of the Cr 3d orbitals, indicative of a Cr³⁺-Cr⁴⁺ hole mechanism. It can account for the increase in conductivity observed in $CuCr_{1-x}Mg_xO_2$ compounds where Cr⁴⁺ holes are formed by the substitution of Mg²⁺ in the matrix of Cr³⁺. Subsequently, calculations based on densityfunctional theory showed that the Cu and Cr 3d states at or near VBM or $E_{\rm f}$ exhibit a strong covalent interaction with O 2pstates, forming delocalized holes in CuCrO₂ and yielding high electronic conductivity.^{8–10} However, more recent theoretical studies by Scanlon and Watson proposed that the Cu¹⁺-Cu²⁺ hole mechanism is more prominent than the Cr³⁺-Cr⁴⁺ hole mechanism in CuCrO₂.¹¹ They also showed that the DOS at the VBM or E_f is composed mainly of the Cu 3d states in CuCrO₂. Experimentally, x-ray emission spectroscopy (XES) revealed that the DOS at the top of the valence band in the Cu-based delafossites is dominated by the Cu 3d character. 12

More recently, Ling et al. found that Cr deficiency increases conductivity by more than 2 orders of magnitude in Crdeficient $CuCr_{1-x}O_2$ (x = 0-0.1) compounds.¹³ They also reported that the Seebeck coefficient is positive, confirming that the p-type holes govern the transport in these compounds. Despite the extensive investigations mentioned above, the relevant path responsible for the p-type hole conduction remains controversial. To address this issue, x-ray absorption near-edge structure (XANES), extended x-ray absorption fine structure (EXAFS), valence-band photoemission spectroscopy (VB-PES), and XES were employed to elucidate the correlation between the electronic or atomic structures and the p-type conductivity of the Cr-deficient $CuCr_{1-x}O_2$ (x = 0-0.1) compounds. The samples studied were prepared by the standard solid-state reaction. Their structural, transport, and magnetic properties have been characterized in detail elsewhere. 13 XANES, EXAFS, VB-PES, and XES experiments have also been described in detail in the Supplementary Material.⁴ The results clearly reveal that the hole-conduction mechanism involves Cu¹⁺-O-Cu²⁺ rather than Cr³⁺-Cr⁴⁺ or direct Cu¹⁺-Cu²⁺ paths.

Figure 1(a) presents normalized O K-edge XANES spectra of the $CuCr_{1-x}O_2$ (x=0-0.1) samples and the Cu_2O , CuO, Cr_2O_3 , and CrO_2 references at room temperature (RT). Since the surface of CrO_2 is easily contaminated with Cr_2O_3 , ¹⁴ the O K-edge XANES spectrum of reference CrO_2 was taken from the literature. ¹⁵ Note that the features of the references are consistent with those reported elsewhere. ^{14–16} The general line shape and threshold energy of the O K-edge XANES spectra of $CuCr_{1-x}O_2$ differ from those of reference CuO and CrO_2 . The spectra of the $CuCr_{1-x}O_2$ samples display four major near-edge features, labeled A_1 – D_1 , which are centered at \sim 530, 533, 535, and 542 eV, respectively. These features provide detailed

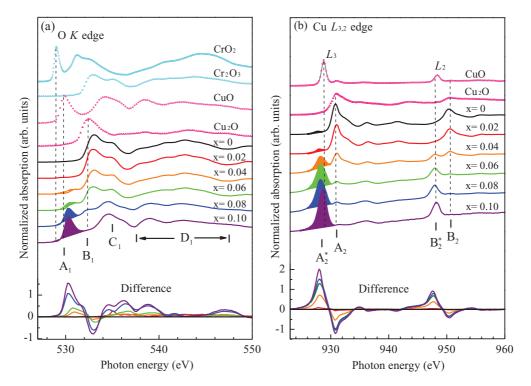


FIG. 1. (Color online) (a) O K-edge XANES spectra of samples studied and the CrO₂, Cr₂O₃, CuO, and Cu₂O reference materials. The bottom panel shows the difference in spectra of CuCr_{1-x}O₂ samples between x = 0.02-0.1 and x = 0. (b) Cu $L_{3,2}$ -edge XANES of CuCr_{1-x}O₂ and reference CuO and Cu₂O samples. The bottom panel shows the difference in spectra of CuCr_{1-x}O₂ samples between x = 0.02-0.1 and x = 0.

information about unoccupied O 2p-derived states above $E_{\rm f}$ in $CuCr_{1-x}O_2$. The main general features at the O K edge for the low Cr-deficient (x = 0 and 0.02) samples is similar to that of the superposed spectra of Cr₂O₃ and Cu₂O with a dominant contribution from Cr₂O₃. They include three features, B₁–D₁, which are attributable to O 2p states that are hybridized with Cr/Cu 3d and 4sp states. Specifically, features B₁ and C₁ are attributable mostly to the O 2p-Cr 3d hybridized states with a small contribution from O 2p-Cu 3d hybridized states based on the theoretical calculations for CuCrO₂.^{8,9} Feature A_1 centered at \sim 530 eV, which is also observed in the CuO spectrum, emerges as x increases from 0.04 to 0.1. The bottom of Fig. 1(a) presents the difference in spectra between the x =0.02 - 0.1 and x = 0 samples. Note that the intensity variation in feature A_1 is opposite that of feature B_1 with increasing Cr deficiency. It suggests that the O K-edge XANES spectral feature is dominated by O 2p and Cu¹⁺/Cr³⁺ 3d hybridized states for the low Cr-deficient samples with x = 0 and 0.02 and then by O 2p and Cu²⁺/Cr³⁺ 3d hybridized states for the high Cr-deficient samples with x = 0.04 - 0.1. As x increases, the emergence of feature A₁, accompanied by the reduction of the intensity of feature B₁, is caused by the formation of unoccupied O 2p-Cu²⁺ 3d hybridized states, indicative of the presence of excess holes at the O sites due to the generation of Cu²⁺. ^{17,18} Furthermore, the absence of a sharp feature at \sim 529 eV, associated with CrO₂ in the spectra of the samples studied, suggests that the O 2p-Cr⁴⁺ 3d hybridized states may not exist in the $CuCr_{1-x}O_2$ samples.

Figure 1(b) displays the normalized Cu $L_{3,2}$ -edge XANES spectra of CuCr_{1-x}O₂ (x = 0-0.1) and reference CuO and

Cu₂O at RT. The bottom panel of Fig. 1(b) presents the difference in spectra between the x = 0.02 - 0.1 and the x = 0 samples. It includes two dominant features, A_2^*/A_2 and B_2^*/B_2 , in the energy range of 924–936 eV and 942–956 eV, which, by the dipole-transition selection rules, correspond to Cu L_3 $(2p_{3/2} \rightarrow 3d)$ and L_2 $(2p_{1/2} \rightarrow 3d)$ transitions, respectively. The main feature in the Cu $L_{3,2}$ -edge XANES spectra of the $CuCr_{1-x}O_2$ samples changes significantly as x increases. The low Cr deficiency samples with $x \le 0.02$ have similar spectral features to that of Cu₂O (Cu¹⁺) with dominant features A_2 and B_2 at the L_3 and L_2 edges, respectively, which supports the dominance of the Cu1+ valence in the low Cr-deficient samples with x = 0 and 0.02. As x increases from 0.04 to 0.1, features A_2^* and B_2^* appear at the Cu $L_{3,2}$ edge, and a similar characteristic feature is observed in the CuO (Cu²⁺) spectrum. The observed changes in the spectral features at the Cu $L_{3,2}$ edge confirm the gradual change in the Cu valence from Cu^{1+} to Cu^{2+} as x increases from 0 to 0.1 in the $CuCr_{1-x}O_2$ samples. This result is consistent with that of the O K-edge XANES shown in Fig. 1(a), suggesting that the gradual change in the Cu valence from Cu¹⁺ to Cu²⁺ with increasing Cr deficiency is caused by the generation of excess holes at the Cu sites $(Cu^{2+}/Cu^{1+}\underline{L},\underline{L})$ denotes the O 2p ligand hole), which are linked to the O sites arising from the strong hybridization between Cu 3d and O 2p states in the CuCr_{1-x}O₂ compounds.

Figure 2(a) presents the Cr $L_{3,2}$ -edge XANES spectra of the samples investigated and the Cr₂O₃ and CrO₂ (the spectrum referred by Ref. 15) at RT. The bottom panel of Fig. 2(a) shows the difference in spectra of CuCr_{1-x}O₂ samples between x = 0.02 - 0.1 and x = 0. Since the energy separation between

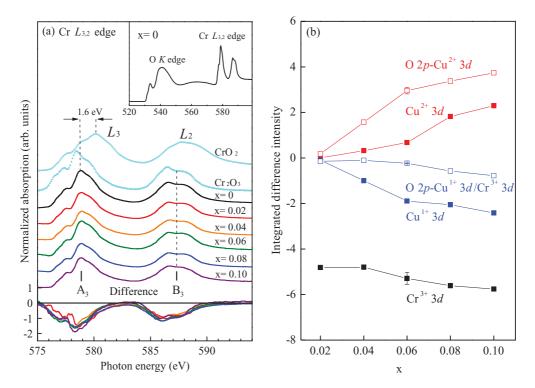


FIG. 2. (Color online) (a) Cr $L_{3,2}$ -edge XANES spectra of samples studied and the CrO₂ and Cr₂O₃ reference materials. The upper inset shows O K- and Cr L_{3} -edge XANES spectra of the x=0 sample. The bottom panel presents the difference in the spectra of the CuCr_{1-x}O₂ samples between x=0.02-0.1 and x=0. (b) Integrated difference intensities of O K-, Cu, and Cr L_{3} -edge XANES spectra of CuCr_{1-x}O₂ versus the Cr deficiency.

the O K and the Cr L_3 edge in the CuCr_{1-x}O₂ spectrum is approximately 50 eV, as presented in the upper inset of Fig. 2(a), the Cr $L_{3,2}$ -edge XANES was carefully normalized by matching the absorption coefficients in the region from 2 eV below the L_3 edge to 10 eV above the L_2 edge and was kept in the same area in the energy range between 595 and 598 eV to avoid a mix up with the O K postedge absorption. Notably, both spectra of CuCr_{1-x}O₂ and Cr₂O₃ exhibit dominant broad features, A_3 and B_3 , centered at \sim 579 and 587 eV, which are attributable to Cr L_3 ($2p_{3/2} \rightarrow 3d$) and L_2 (2 $p_{1/2} \rightarrow 3d$) transitions, respectively. The general spectral features in the $CuCr_{1-x}O_2$ samples bear a resemblance to those of Cr₂O₃ (Cr³⁺) rather than CrO₂ (Cr⁴⁺) and the dominant broad features A₃ and B₃ of CuCr_{1-x}O₂ shift to lower energy by ~ 1.6 eV than those of CrO₂, indicating the dominance of the Cr³⁺ oxidation state and an absence of the Cr⁴⁺ valence in the CuCr_{1-x}O₂ samples. This finding is consistent with the result deduced from the O K-edge XANES spectra described above.

Figure 2(b) plots the integrated difference intensities of features A_1 (O 2p-Cu²⁺ 3d) and B_1 (O 2p-Cu¹⁺/Cr³⁺ 3d) at the O K edge, features A_2^* (Cu²⁺) and A_2 (Cu¹⁺) at the Cu L_3 edge, and feature A_3 (Cr³⁺) at the Cr L_3 -edge XANES spectra as a function of the Cr deficiency x. The intensities of the features associated with the O 2p-Cu¹⁺/Cr³⁺ 3d hybridized states and the Cu¹⁺ 3d valence states gradually decrease, those of the features associated with the O 2p-Cu²⁺ 3d hybridized states in the O K-edge spectra and the Cu²⁺ valence states in the Cu L_3 -edge spectra increase, and those of the features associated with the Cr³⁺ valence states derived from the Cr

 L_3 -edge spectra decrease as x increases. The results shown in Fig. 2(b) along with the temperature-dependent Cr $L_{3,2}$ -edge XANES spectra (see the Supplementary Material of Fig. S2 in Ref. 4) unambiguously show the absence of the Cr⁴⁺ valence in the $CuCr_{1-x}O_2$ compounds. It rules out the Cr^{3+} - Cr^{4+} hole mechanism as a possible scenario for transport properties of samples studied. In contrast, the underlying origin of the ptype conduction in the $CuCr_{1-x}O_2$ samples is, therefore, hole doping at the Cu/O sites. These excess holes are expected to hop from one Cu to another Cu site through a process of $Cu^{1+} 3d$ -O 2p- $Cu^{2+} 3d$. The variations in the intensities with increasing Cr deficiency inferred from the O K-, Cu, and Cr L_3 -edge spectra suggest that the enhanced p-type conduction is associated with the itinerant "hole doping" and "electron transfer" from the Cu 3d orbitals through the Cu¹⁺-O-Cu²⁺ dumbbell bridges to the Cr3+O2 octahedral layers, acting as a reservoir for electrons. 19

Figure 3(a) displays the VB-PES spectra of $CuCr_{1-x}O_2$ (x=0-0.1) obtained with a photon energy of 150 eV. Striking differences were observed between the VB-PES spectra of the Cr-deficient samples with x=0.02-0.1 and that of the Cr-deficiency-free sample, i.e., x=0. Since the photoionization cross section of Cu 3d is four times as large as that of Cr 3d at an excitation photon energy of $h\nu=150$ eV, 20 the three major features, A_4-C_4 in the spectra of $CuCr_{1-x}O_2$ shown in Fig. 3(a) are primarily attributable to Cu 3d and O 2p-Cu 3d hybridized states and O 2p bonding states, 8,9 although the valence band of $CuCrO_2$ is almost entirely composed of the Cr 3d states due to the strong hybridization between Cr 3d and O 2p orbitals. 6,10 Apparently, the intensity of feature C_4

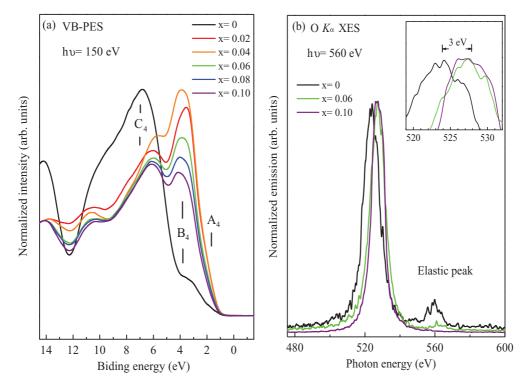


FIG. 3. (Color online) (a) VB-PES spectra of $CuCr_{1-x}O_2$ (x = 0-0.1). (b) O K_{α} XES spectra of $CuCr_{1-x}O_2$ (x = 0,0.06, and 0.1). The upper inset magnifies the main feature of the XES spectra. Note that a satellite feature at ~ 560 eV is an elastic peak.

of the samples with x = 0.02-0.1 is much lower than that of the sample with x = 0, and the intensities of features A_4 and B₄ are significantly higher. These changes indicate that the O 2p valence electrons shift to the more delocalized O 2p-Cu 3d and localized Cu 3d states to create holes and to enhance the conductivity for the Cr-deficient samples. Figure 3(b) presents the O K_{α} XES spectra obtained at an excitation energy of 560 eV, which include a main feature centered at \sim 524 eV for x = 0 and 527 eV for x = 0.06 and 0.1 associated with the O 2p states below VBM or E_f . As x increases from 0 to 0.06 and 0.1, the feature associated with the O 2p states is shifted to the higher energy by \sim 3 eV as displayed in the upper inset of Fig. 3(b), suggesting the shift in the DOS of O 2ptoward VBM or E_f . This shift is consistent with the VB-PES results shown in Fig. 3(a), which shows an \sim 3 eV shift from the intensity maximum of feature C_4 of the x = 0 sample to that of feature B_4 of the x = 0.02-0.1 samples. The overall drop in the intensities of features A₄ and B₄ with increasing Cr deficiency shown in Fig. 3(a) strongly indicates an increase in the number of Cr-deficiency-doped holes at the Cu sites, accompanied by a decrease in DOS at or near VBM or $E_{\rm f}$.

To shed light on the temperature-dependent p-type electrical conduction in $\text{CuCr}_{1-x}\text{O}_2$, $\ln(\rho)$, as a function of temperature for samples studied, is displayed in Fig. 4(a). A deviation from T-linear behavior in the $\ln(\rho)$ -T plot below \sim 250 K suggests that there is a crossover electrical conduction mechanism around 250 K. In the temperature region of \sim 250 K < T < 300 K, experimental data fit well to straight dashed lines, indicative of a strong support of the thermally activated (TA) mechanism with $\rho(T) = \rho_0 \exp[(E_{\text{TA}}/kT)]$, where E_{TA} denotes the activation energy. The estimated E_{TA} value determined from the slopes of these straight lines

increases from ~ 0.07 eV for the x = 0.1 sample to ~ 0.28 eV for the x = 0 sample as shown in the inset of Fig. 4(a). The values of E_{TA} are much smaller than the reported band gap (E_g) value of 2.95–3.30 eV,¹¹ indicating that the thermally excited electrons are transferred into shallow acceptor or defect states in the gap²¹ as presented schematically in Fig. 4(b), rather than a conduction-band minimum (CBM). A higher Cr-deficiency sample with a smaller E_{TA} makes valence electrons easy to excite into the shallow acceptor or defect states. It correspondingly increases the number of holes in the valence band and gives rise to a higher conductivity. These findings not only agree with the reported results that the holes govern charge transport in $CuCr_{1-x}O_2$ compounds, ¹³ but also consistently reconcile the reduction in DOS at or near VBM or E_f and the increase in the Cu²⁺ valence state as x increases, discussed above. In the temperature region of \sim 130 K <T < 250 K, $\rho(T)$ follows a combination of the TA and three-dimensional variable range hopping (3D-VRH) model with the expression $\rho(T) \propto \exp[E_{\text{TA}}/kT] + \exp[(T_0/T)^{1/4}]$ displayed in the solid curves in Fig. 4(a), where $T_0 \propto 1/a^3$ and a is the localization length of carriers.²² It suggests that the Mott's VRH mechanism participates in charge transport between ~ 130 K and 250 K and the p-type conductivity is still partially contributed by thermally activated valence electrons that create holes in the valence band.

To get a better understanding of the temperature-dependent p-type conductivity in the $CuCr_{1-x}O_2$ samples, the temperature-dependent $Cu\ L_{3,2}$ -edge XANES spectra of $CuCr_{1-x}O_2$ (x=0,0.06, and 0.1) and reference CuO and Cu_2O at RT are shown in the Supplementary Material of Figs. S3(a)–S3(c) in Ref. 4. They exhibit features similar to those of A_2/A_2^* and B_2/B_2^* in the $Cu\ L_{3,2}$ -edge spectra

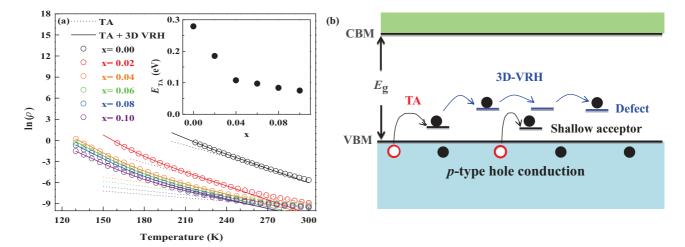


FIG. 4. (Color online) (a) $\ln(\rho)$ versus T for $\operatorname{CuCr}_{1-x}\operatorname{O}_2(x=0-0.1)$: Open circles represent experimental data, dotted lines represent fitting by TA conduction, and solid lines represent fitting by a combination of the TA and 3D-VRH mechanisms. (b) A schematic illustrates the TA and 3D-VRH conductions.

shown in Fig. 1(b). As shown in the bottom panels of Figs. S3(a)–S3(c), the intensities of the Cu $L_{3,2}$ edge features overall decrease with decreasing temperature, indicative of a decrease in the number of unoccupied Cu 3d states. More interestingly, as temperature increased from 90 K up to RT, a gradual valence state change from Cu¹⁺ to Cu²⁺ was observed for the x = 0.06 sample, in contrast, the amount of Cu¹⁺ in the x = 0 sample, nearly kept constant, and that of Cu²⁺ in the x = 0.1 samples increased. This finding reveals that the p-type carrier conduction assisted by thermal excitation for samples with higher Cr deficiency becomes more pronounced at high temperatures. As a result, it increases the number of holes at the Cu/O sites, causing more Cu¹⁺ to become Cu²⁺ and significantly enhances p-type conductivity

at high temperatures. Additionally, according to the analysis of the EXAFS data [also see Figs. S4(a) and S4(b) in the Supplementary Material (Ref. 4)], no substantial variation in the Cu-O and Cu-Cu bond distances with x was observed in the $\text{CuCr}_{1-x}\text{O}_2$ samples. The result clearly suggests that the observed changes in the p-type conductivity over a wide range of temperatures predominantly arise from changes in the electronic structures not the Cu-O and Cu-Cu bond distances.

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^{*}Present address: Department of Physics, National Taiwan University, Taiwan.

[†]Author to whom all correspondence should be addressed: dcling@mail.tku.edu.tw

[‡]wfpong@mail.tku.edu.tw

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