



## 中文摘要

薄膜溶劑萃取裝置主要藉一微孔薄膜將兩液相隔離，而溶質自萃餘相通過薄膜而傳入萃取相。本研究就回流效應對交流式平板型薄膜萃取器效率之影響，作理論與實驗之探討。質量傳送之理論分析，乃類比熱交換器中之熱傳送。實驗係藉微孔聚丙烯所製成之薄膜，作為可通過之隔網，並利用甲基異丙酮為溶劑，在各種溶液濃度與流率以及回流比下，萃取水中之醋酸。理論推測值與實驗值甚為吻合。本研究並證實回流操作，確能顯著提高萃取效率。

當液相(萃餘相或萃取相)之分佈係數較大及溶液濃度較高時，質量傳送之阻力主要受此相所控制，此時薄膜萃取器若加設回流裝置，可增強流體速度而減小其質量傳送阻力，進而提高萃取效率。

薄膜萃取操作優於傳統萃取操作，蓋因前者可以克服後者的這些缺點：氾濫、混合、兩相密度差、液相流速之互相牽制…等。因此薄膜萃取之研究，乃目前分離程序中相當熱門之一環，而本研究所推介之可提高萃取效率的回流效應，可促使薄膜萃取操作之應用更為廣泛。

## A Study on The Performance of Crossflow Flat-Plate Membrane Extractions

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### ABSTRACT

The effects of recycle on membrane extraction through a cross-flow rectangular module have been studied both theoretically and experimentally. Theoretical analysis of mass transfer in cross-flow device with and without recycle was analogous to heat transfer in cross-flow heat exchangers. Experiments were carried out with the use of a membrane sheet made of microporous polypropylene as a permeable barrier to extract acetic acid from aqueous solution by methyl isobutyl ketone. Theoretical predictions are in agreement with the experimental results. Contrast a device without recycle, improvement in mass transfer is achievable if cross-flow membrane extraction is operated in a device of same size with recycle which provides the increase of fluid velocity, resulting in reduction of mass-transfer resistance.

**Keywords:** Solvent extraction; Microporous membrane; Recycle effect; Cross flow

### Introduction

The performance of membrane solvent extraction through rectangular mass exchangers has been discussed in the previous work (Yeh and Hsu, 1999; Yeh and Chen, 2000), under cocurrent-flow, countercurrent-flow and cross-flow operations. Though many research works concerning microporous membrane extraction have been reported (Kiani et al., 1984; Basu & Sirkar, 1991; Ding & Cussler, 1991) none of them have considered the effects of recycle of the fluids at the ends. Recently, the effect of recycle on the performance in parallel-flow devices was first investigated by Teramoto et al. (1994), and was later reported by the present author (Yeh, et al., 1998). It was found in previous work that recycle can enhance the mass transfer in parallel-flow rectangular membrane extractors, especially for operations with higher inlet volume rate or shorter conduit length. It is the purpose of present work to investigate theoretically and experimentally the effects of recycle on mass transfer through cross-flow rectangular membrane extractors.

### 2.Theory

Fig. 1 shows the membrane extraction system, in which an impermeable plate with negligible thickness is placed in vertical to the upper plate and the membrane sheet at the center line of channel a (phase a), to divide the channel

into two subchannels ( subchannels  $a_1$  and  $a_2$ ) of same size, and a pump is installed for recycle. Before entering the subchannels  $a_1$ , for double-

pass system with a recycle at the inlet, the raffinate phase (phase a) with inlet volume rate  $Q_a$  and concentration  $C_{a,i}$ , will mix the fluid exiting from subchannel  $a_2$  with volume rate  $RQ_a$ , which is controlled by means of a conventional pump situated at the beginning of subchannel  $a_1$ . The extraction phase (phase b) with inlet volume rate  $Q_b$  flows steadily through channel b. The total mass transfer area of membrane surface,  $S=B \times L=2(L \times B/2)$ , are the same for both devices with and without recycle, as shown in the figure.

#### 2.1. Governing equations

Fig. 1 illustrates the flows in a cross-flow membrane extractor with recycle. The expressions for mass transfer rates are

$$W=Q_a(C_{a,i}-C_{a,e})=(1+R)Q_a(C_{a,i}^0-C_{a,e}) \quad (1)$$

$$=Q_b(C_{b,e}-C_{b,i}) \quad (2)$$

Since the impermeable plate divides the raffinate phase into two flow regions, mass balances will be also taken for each flow region. By taking the mass balances through a differential area  $dx dy$  in flow region 1, one obtains

$$-[(1+R)Q_a/(B/2)]dydC_{a,i}$$

$$=Kdx dy(H_{ac}C_{a,i} - H_{bc}C_{b,i}) \quad (3)$$

$$=[(Q/L)dx]dC_{b,i} \quad (4)$$

Similarly, for flow region 2

$$[(1+R)Q_a/(B/2)]dydC_{a,2}$$

$$=Kdx dy(H_{ac}C_{a,2} - H_{bc}C_{b,2}) \quad (5)$$

$$=[(Q/L)dx]dC_{b,2} \quad (6)$$

The boundary conditions for solving  $C_{a,1}$ ,  $C_{a,2}$ ,  $C_{b,1}$  and  $C_{b,2}$  from Eqs.(3)-(6) are:

$$\text{at } x=0, C_{a,1} = C_{a,i}^0, C_{a,2} = C_{a,e} \quad (7),(8)$$

$$\text{at } x=L, C_{a,1} = C_{a,2} = C_{a,le} \quad (9),(10)$$

$$\text{at } y=0, C_{b,1} = C_{b,i} \quad (11)$$

$$\text{at } y=B/2, C_{b,1} = C_{b,le} \quad (12)$$

$$\text{at } y=B, C_{b,2} = C_{b,e} \quad (13)$$

Inspection of Eqs.(7)-(13) shows that the outlet concentrations,  $C_{a,le}$ ,  $C_{a,e}$ ,  $C_{b,le}$ , as well as the mixed inlet concentration,  $C_{a,i}^0$ , are not specified

a priori. Mathematically, more relations for mass-transfer rates in regions 1 and 2, as well as for the mixing effect at the inlet, are needed for determination of these values. They are

$$(1+R)Q_a(C_{a,i}^0 - C_{a,le}) = Q_b(C_{b,le} - C_{b,i}) \quad (14)$$

$$(1+R)Q_a(C_{a,le} - C_{a,e}) = Q_b(C_{b,e} - C_{b,le}) \quad (15)$$

$$C_{a,i} + RC_{a,e} = (1+R)C_{a,i}^0 \quad (16)$$

Solving above equations one obtains the equation for mass transfer rate as

$$W = (1+R)AQ_a [C_{a,i} - (H_{bc}/H_{ac})C_{b,i}] \quad (17)$$

where

$$A = \frac{1 - \left( \frac{\lambda(1+R)}{n} + \lambda(1+R) + \frac{1}{1-e^{-\lambda(1+R)}} - \frac{\lambda(1+R)}{1-e^{-\lambda n^2}} \right) B}{(1+R) - \frac{\lambda(1+R)}{n} - \frac{1}{1-e^{-\lambda(1+R)}} + \frac{\lambda(1+R)}{1-e^{-\lambda n^2}}} \quad (18)$$

$$B = \left[ \frac{\lambda(1+R)}{1-e^{-\frac{\lambda n^2}{2}}} + \frac{1}{1-e^{-\frac{\lambda n}{2(1+R)}}} - \frac{2(1+R)}{n} \right]^{-1} \quad (19)$$

$$\ell = \frac{Q_a H_{bc}}{Q_b H_{ac}} \quad (20)$$

$$n = \frac{KSH_{ac}}{Q_a} \quad (21)$$

### 3. Experiment

#### 3.1. Experimental performance

The chemical, materials, dimensions of apparatus and experimental procedure are

exactly the same as those employed and performed in previous work (Yeh and Chen, 2000), except that in present study, a two-pass membrane extractor with recycle (see Fig.1), instead of a single-pass membrane extractor without recycle, was employed. Experiments were carried out with the use of a membrane sheet ( $L=B=16.5$  cm) made of microporous polypropylene (Gelman sciences, average pore size of  $0.2 \mu\text{m}$ , porosity of 70% and thickness of  $178 \mu\text{m}$ ) as a permeable barrier to extract acetic acid (reagent ACS grade, Fisher) from aqueous solution by methyl isobutyl ketone (MIBK, reagent grade, Fisher). The membrane sheet was inserted between two horizontally parallel plates of stainless steel, with same distance from them to divide the conduit into two channels (channels a and b, or phases a and b) of same height ( $h=0.19$  cm). For membrane extraction with recycle, an impermeable plate was placed additionally in vertical to the upper plate and the membrane sheet at the centerline of channel a to divide channel a into two subchannels (subchannels a and b) of height  $h$  and width  $(B/2)$  for recycle, as shown in Fig. 1.

#### 3.2 Comparison of theoretical predictions with experimental results

The experimental conditions are as follows. Aqueous solution:  $Q_a=0.184\sim 1.426$   $\text{cm}^3/\text{s}$ ;  $C_{a,i}=4.96 \times 10^{-4}$ ,  $2.02 \times 10^{-3}$   $\text{mole}/\text{cm}^3$ . Organic solution:  $Q_b=0.125$   $\text{cm}^3/\text{s}$ ;  $C_{b,i}=0$ . Since acetic-acid aqueous solution (phase a) and MIBK organic solution (phase b) employed in present experimental work are immiscible, it does not need to fill another fluid (phase c) in the pores of the membrane. Further, microporous polypropylene used in present experiment is hydrophobic membrane, the organic solution wets the membrane, and thus  $H_{bc}=1$  and  $H_{ac}=0.524$  at  $25^\circ\text{C}$  (Yeh and Huang, 1995). Some experimental results of  $C_{a,e}$  were obtained and the experimental values of mass transfer rate,  $W$ , were calculated from Eq. (1). The results for  $W$  are plotted in Figs. 2 and 3.

The theoretical predictions were calculated from Eq. (17) with the use of the following correlation equations for overall mass transfer coefficients (Yeh and Chen, 2000):

$$K \times 10^4 (\text{cm}/\text{s}) = 7.256 V_a^{0.104}, \text{ for } C_{a,i} = 4.96 \times 10^{-4} \text{ mole}/\text{cm}^3; \quad (22)$$

$$K \times 10^4 (\text{cm}/\text{s}) = 4.734 V_a^{0.124}, \text{ for } C_{a,i} = 2.02 \times 10^{-3} \text{ mole}/\text{cm}^3; \quad (23)$$

, as well as the relation of  $V_a$  to  $Q_a$  ( $\text{cm}^3/\text{s}$ )

$$V_a = \frac{Q_a(1+R)}{h(B/2)} = \frac{Q_a(1+R)}{(0.19)(165/2)}, \text{ cm/s} \quad (24)$$

The results of theoretical prediction are also plotted in Figs. 3 and 4 for comparison. It is seen from these figures that the theoretical predictions are in agreement with the experimental results.

#### 4. Conclusion

The improvement of performance in membrane extraction by operating a device with recycle is best illustrated by calculating the percentage increase in mass-transfer rate based on the operation in a device of same size without recycle

$$I = \frac{W - W_0}{W_0} \quad (25)$$

The experimental values of  $W_0$  and  $W$  were used to calculate  $I$  by Eq. (25), and the results are presented in Table 1. From these results we see that operation with recycle of higher reflux ratio substantially improves the mass transfer rate. The enhancement increases with increasing reflux ratio, especially for larger inlet concentration  $C_{a,i}$  in raffinate phase.

#### Nomenclature

B	membrane width (cm)
$C_{a,1}, C_{a,2}$	solute concentration distribution in channel $a_1$ , in channel $a_2$ , of raffinate phase (mole/cm <sup>3</sup> )
$C_{b,1}, C_{b,2}$	solute concentration distribution within $0 \leq y \leq B/2$ , within $B/2 \leq y \leq B$ , of extract phase (mole/cm <sup>3</sup> )
$C_{a,i}, C_{b,i}$	inlet solute concentration in phase a, in phase b (mole/cm <sup>3</sup> )
$C_{a,e}, C_{b,e}$	outlet solute concentration in phase a, in phase b (mole/cm <sup>3</sup> )
$C_{a,1e}, C_{b,1e}$	solute concentration of phase a at $x = L$ , of phase b at $y = B/2$ (mole/cm <sup>3</sup> )
$C_{a,i}^0$	mixed inlet concentration in raffinate phase (mole/cm <sup>3</sup> )
$H_{ac}, H_{bc}$	distribution coefficient between phase a and phase c, between phase b and phase c
h	height of flow channel (cm)
I	improvement of mass-transfer rate defined by Eq. (24)
K	overall mass-transfer coefficient (cm/s)
L	length of membrane sheet. (cm)
$\ell, n$	dimensionless group de-fined

$Q_a, Q_b$	by Eq.(20), by Eq.(21) volume flow rate in phase a, in phase b (cm <sup>3</sup> /s)
R	reflux ratio
S	total mass-transfer area in a membrane sheet, BL (cm <sup>2</sup> )
W	total mass-transfer rate in a membrane extractor (mole/s)
$W_0$	W obtained in a device of same size without recycle (mole/s)
x, y	rectangular coordinates (cm)
$V_a, V_b$	fluid velocity in phase a, in phase b (cm/s)

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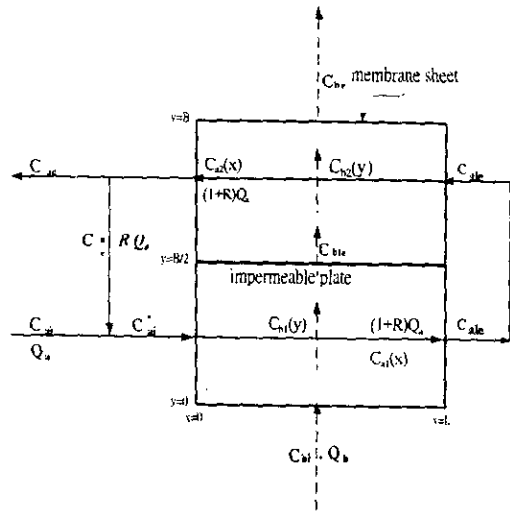


Fig.1. Double-pass cross-flow flat-plate membrane extractor with recycle

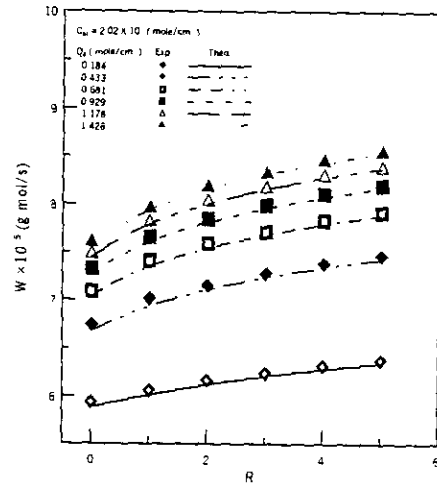


Fig.3.  $W$  vs.  $R$ :  $C_{a,i} = 2.02 \times 10^{-3}$  mole/cm<sup>3</sup>;  $Q_b = 0.125$  cm<sup>3</sup>/s

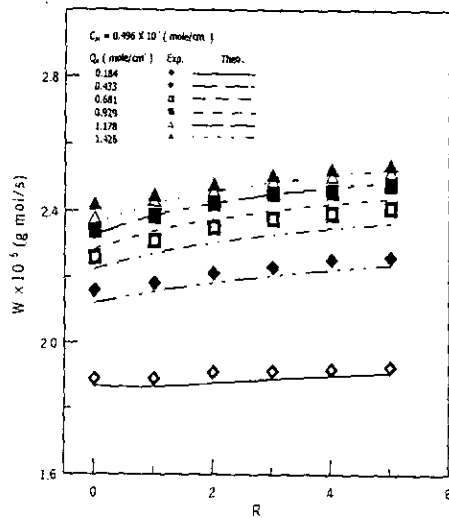


Fig.2.  $W$  vs.  $R$ :  $C_{a,i} = 0.496 \times 10^{-3}$  mole/cm<sup>3</sup>;  $Q_b = 0.125$  cm<sup>3</sup>/s

Table 1

Experimental values of  $W_n$  (Yeh & Chen, 2000) and  $I$  for water-acetic acid-MIBK system obtained with  $Q_b = 0.125$  cm<sup>3</sup>/s and  $C_{b,i} = 0$

$C_{a,i} \times 10^3$ (mole/cm <sup>3</sup> )	$Q_a$ (cm <sup>3</sup> /s)	$W_n \times 10^5$ (mole/s)	$I$ (%)		
			$R=1$	$R=3$	$R=5$
0.496	0.184	1.9670	-3.84	-1.33	-1.91
	0.433	2.1044	3.72	6.05	7.49
	0.681	2.2064	4.72	7.84	9.32
	0.929	2.2575	5.68	8.72	9.96
	1.178	2.3560	3.30	5.85	7.05
	1.426	2.4527	-1.15	2.38	3.66
2.02	0.184	6.1401	-1.24	1.70	3.92
	0.433	6.5037	7.93	11.90	14.78
	0.681	6.9326	6.92	11.30	14.26
	0.929	7.3205	4.62	9.20	12.06
	1.178	7.5274	4.13	8.85	11.61
	1.426	7.6719	4.01	8.74	11.65